

# **Estimating Probability Distribution of Benefit from Flood Control Project**



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**1**

## **TOPICS**

- **Background and Objective**
- **Research method**
- **Application to the Dam construction project**
- **Conclusion**

**2**

## TOPICS

### ● Background and Objective

#### ● Research method

#### ● Application to the Dam construction project

#### ● Conclusion

3

## BACKGROUND AND OBJECTIVE

### Background

- ✓ Increasing risk of severe flood due to climate change
  - It becomes more important to evaluate and manage flood risk.
  - Flood control facilities (dam, bank etc...) are constructed to mitigate flood risk.
  
- ✓ Evaluation of benefit from flood control project
  - In Japan, Cost-Benefit analysis is used to evaluate flood control project.
  - Benefit from flood control project is evaluated by **expected value** of reduced damage cost.
  
- ✓ Uncertainty of benefit from flood control project
  - Especially in highly protected area, flooding doesn't occur frequently, and it is **highly uncertain whether we can get benefit calculated from expected value.**

4

# BACKGROUND AND OBJECTIVE

## Objective

- ✓ Define benefit from flood control project as **random variable** and **estimate its probability distribution**.
- ✓ Reveal the uncertainty of benefit from flood control project and stochastically discuss the efficiency of flood control project from estimated probability distribution.

5

# BACKGROUND AND OBJECTIVE

### Existing Method

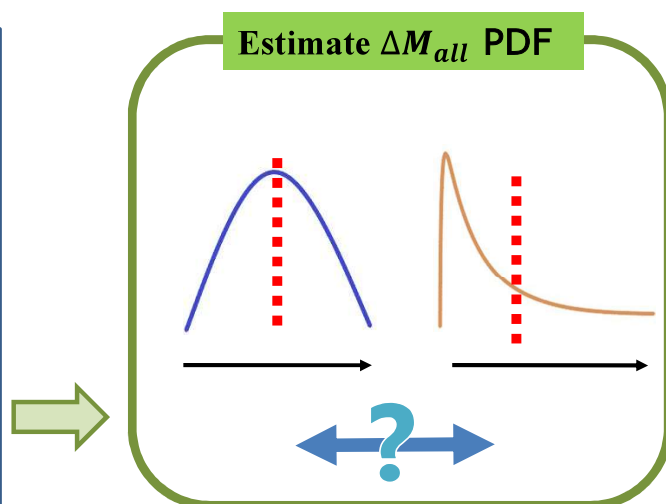
$$B = \sum_{t=1}^T b$$

- $b$  : annual expected reduced damage cost
- $T$  : Evaluation period
- Evaluate by **one value**
- \*neglecting discount rate

### In this research

$$\Delta M_{all} = \sum_{t=1}^T \Delta M_t$$

- $\Delta M_{all}$  :  $T$ -year cumulative reduced damage cost
- $\Delta M_t$  : reduced damage cost of year  $t$
- Redefine benefit as **random variable**  $\Delta M_{all}$



- Expected value of PDF corresponds to the benefit value of existing method (Neglecting discount rate)
- Stochastically discuss the efficiency of flood control project.

6

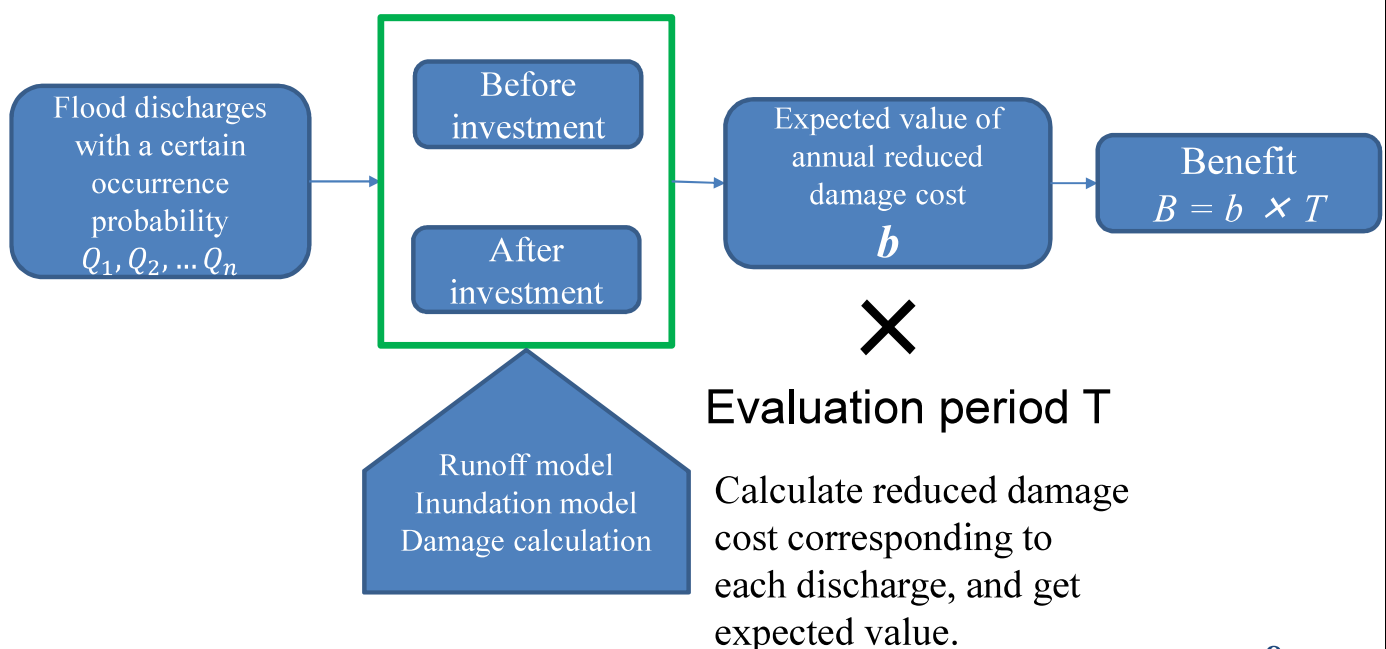
## TOPICS

- Background and Objective
- **Research method**
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- Conclusion

7

## METHOD

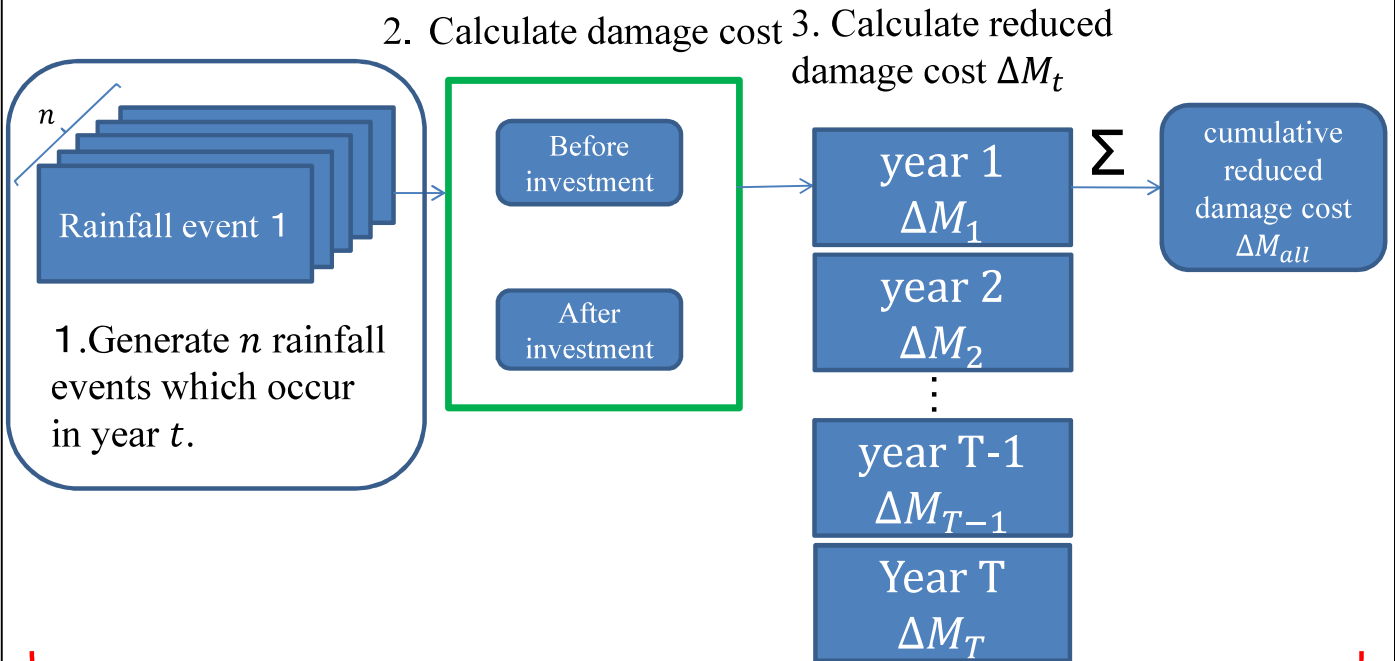
- How to calculate benefit B by the existing method  
Calculate B by using expected value of annual reduced damage cost.  
Efficiency of the flood control project is evaluated by one value, B.



8

## METHOD

Numerically estimate PDF of cumulative reduced damage cost,  $\Delta M_{all}$ .

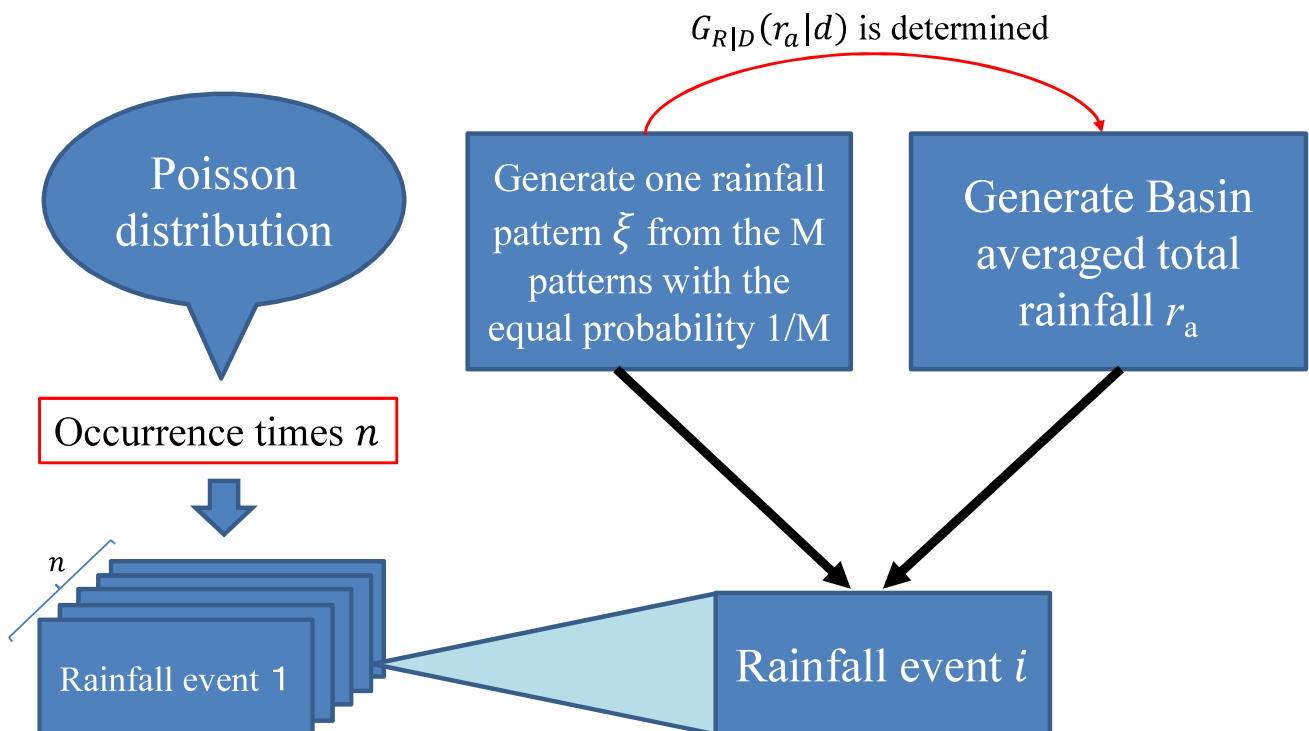


Repeating calculation of cumulative reduced damage cost  $N$  times, and estimate PDF numerically

9

## METHOD

Generation of annual rainfall events



10

# TOPICS

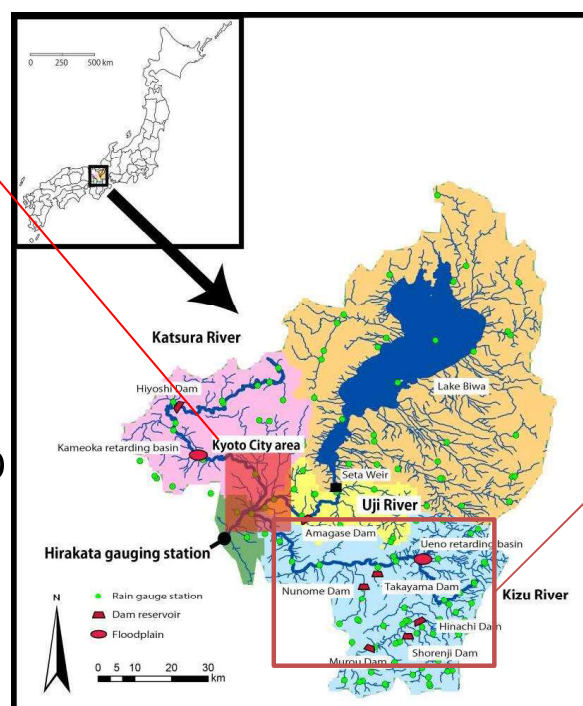
- Background and Objective
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11

## APPLICATION TO THE DAM CONSTRUCTION PROJECT

Calculate the reduced damage cost in the area of the three tributaries' conjunction.

- basin: Yodo basin
- Calculation times N:100,000
- Evaluation period T : 50 years
- Rainfall-runoff/inundation models constructed by the existing research are used.



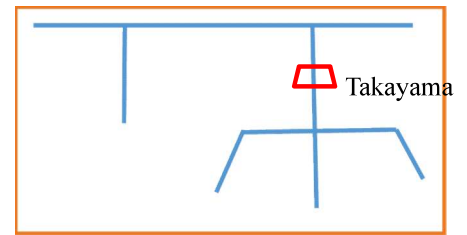
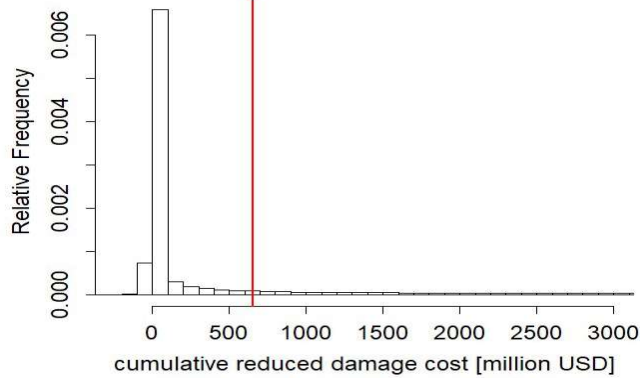
Set several flood control projects about the existing dam reservoirs in upper stream of the river basin

12

# APPLICATION TO THE DAM CONSTRUCTION PROJECT

**Project A** : Constructing Takayama dam

Histogram of  $\Delta M_{all}$  (red line : expected value)



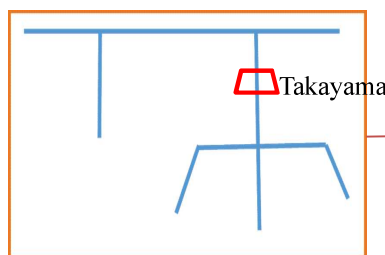
Expected value B	655
$\Pr[\Delta M_{all} \geq B]$	0.18
$\Pr[\Delta M_{all} > 0]$	0.55

- $\Delta M_{all}$  distribution is unsymmetrical, has a long tail.
- it is highly uncertain whether we can get benefit calculated from expected value
- the expected value made it difficult to grasp the whole characteristic of the benefit of the project

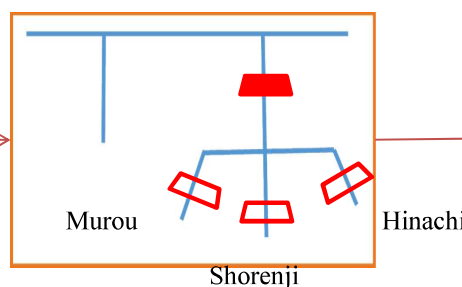
13

# APPLICATION TO THE DAM CONSTRUCTION PROJECT

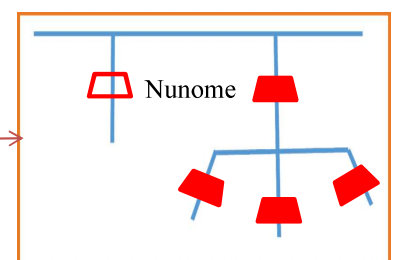
**project A**



**Project B**



**Project C**



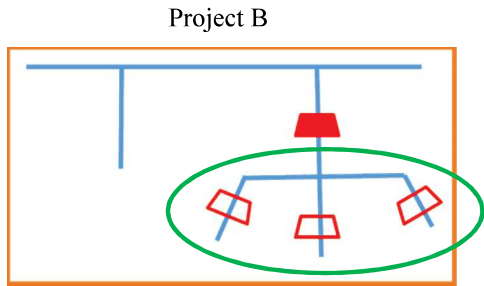
To examine the impact of the location of dams on the estimated probability distribution, we split the construction project of the four dams into projects B, and project C

14

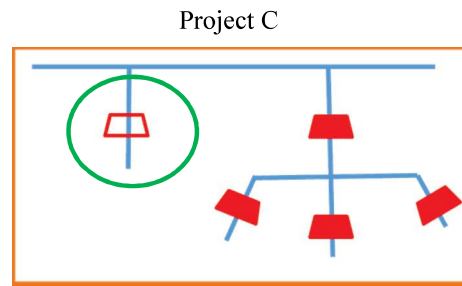
# APPLICATION TO THE DAM CONSTRUCTION PROJECT

	Project A	Project B	Project C
$\Pr[\Delta M_{all} \geq B]$	0.18	0.10	0.23
$\Pr[\Delta M_{all} > 0]$	0.55	0.30	0.74

Project A & Project B: the probability that the dam effect comes out decreases  
 Project B & Project C: the probability that the dam effect comes out increases



Constructing dams on the same tributaries



Another tributary's discharge can be reduced

# APPLICATION TO THE DAM CONSTRUCTION PROJECT

	Project B	Project C
Expected value(B)	197	157
$\Pr[\Delta M_{all} \geq B]$	0.10	0.23
$\Pr[\Delta M_{all} > 0]$	0.30	0.74

Expected value is not so changed, but the probability that the dam effect comes out is doubled.

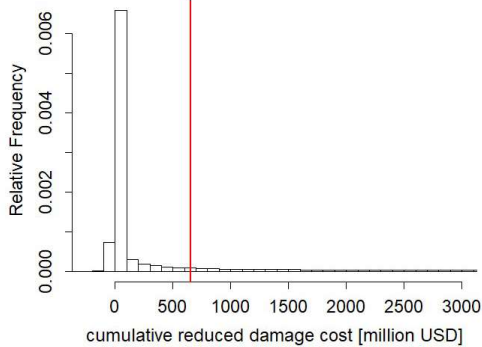
→ Indicating the importance of using some statistics beside expected value when evaluating flood control project.



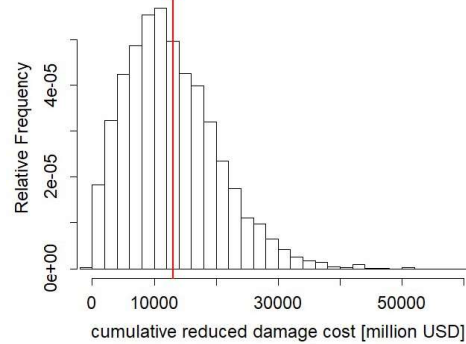
# APPLICATION TO THE DAM CONSTRUCTION PROJECT

- Set longer evaluation period ( $T = 1,000$  year) and estimate the distribution
  - Distribution becomes symmetrical, the probability that  $\Delta M_{all}$  exceeds expected value increases
- The actual evaluation period was not long enough to represent the expected value as the benefit due to low frequency of flooding.

Histogram of  $\Delta M_{all}$  (50 years)



Histogram of  $\Delta M_{all}$ (1000 years)



	Project A (50 years)		Project A (1,000 years)
skewness	38.3	>	8.38
$\Pr[\Delta M_{all} \geq B]$	0.18	<	0.43

17

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18

## CONCLUSION

Develop method of estimating  $\Delta M_{all}$  distribution.

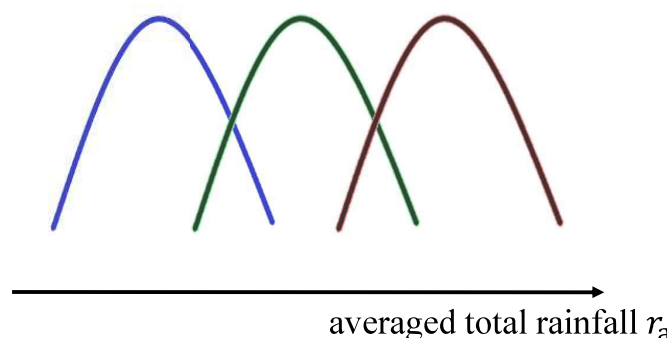
It enables us to stochastically discuss the efficiency of flood control project. In my case study, following findings are obtained.

- ✓  $\Delta M_{all}$  distribution was unsymmetrical, has a long tail.
- ✓ Depending on the projects, some statistics (e.g.  $\Pr[\Delta M_{all} \geq B]$ ) are totally different while expected value is almost the same.
- ✓ The actual evaluation period was not long enough to represent the expected value as the benefit due to low frequency of flooding.

19

## FURTHER APPLICATION

- In this research, rainfall generation was done using the same rainfall distribution every year.
- If you can predict the change of rainfall distribution caused by climate change, you can reflect the impact of climate change on the evaluation process by changing the rainfall distribution for rainfall generation in each stage.



20

# THANK YOU FOR LISTENING !

21

## METHOD

Three assumptions about rainfall are set to generate rainfall event

1. Rainfall pattern
2. Basin averaged total rainfall
3. Annual number of occurrences of rainfall events

1. When rainfall occurs, possible rainfall pattern is limited to the  $N$  patterns. Pattern  $\xi_i$  ( $i = 1, 2, \dots, N$ ) occurs with the same probability  $p$ . Denote rainfall duration time of pattern  $\xi_i$  as  $d_i$ .

2. Basin averaged total rainfall  $r_a$  follows the conditional cumulative distribution function (CDF)  $G_{R_a|D}(r_a|d_i)$  given  $d_i$ .

→ One rainfall event (rainfall intensity at a location  $(x, y)$  and time  $t$ ) is determined by  $r(x, y, t) = r_a \xi(x, y, t)$

3. Annual number of occurrences of rainfall events follows the Poisson distribution with occurrence ratio of  $\mu_a$ .

22